

**2001**

A5. (a) Obtain partial fractions for  $\frac{x}{x^2-1}, x > 1$ . (2)

**2002**

A8. Express  $\frac{x^2}{(x+1)^2}$  in the form  $A + \frac{B}{x+1} + \frac{C}{(x+1)^2}, (x \neq -1)$ , stating the values of the constants  $A, B$  and  $C$ . (3)

**2004**

5. Express  $\frac{1}{x^2-x-6}$  in partial fractions. (2)

**2005**

13. Express  $\frac{1}{x^3+x}$  in partial fractions. (4)

**2007**

4. Express  $\frac{2x^2-9x-6}{x(x^2-x-6)}$  in partial fractions. (3)

**2008**

4. Express  $\frac{12x^2+20}{x(x^2+5)}$  in partial fractions. (3)

**2009**

14. Express  $\frac{x^2+6x-4}{(x+2)^2(x-4)}$  in partial fractions. (4)

**2011**

1. Express  $\frac{13-x}{x^2+4x-5}$  in partial fractions (2)

**2012**

15. (a) Express  $\frac{1}{(x-1)(x+2)^2}$  in partial fractions (2)

**2014**

14. (b) Express  $\frac{1}{3r^2-5r+2}$  in partial fractions. (2)

**2015**

17. Find  $\int \frac{2x^3-x-1}{(x-3)(x^2+1)} dx, x > 3$ . (9)

**2016**

13. Express  $\frac{3x+32}{(x+4)(6-x)}$  in partial fractions

**2017**

2. Express  $\frac{x^2-6x+20}{(x+1)(x-2)^2}$  in partial fractions (4)

**2018**

2. Use partial fractions to find  $\int \frac{3x-7}{x^2-2x-15} dx$ . (4)

**2019**

4. (a) Express  $\frac{3x^2 + x - 17}{x^2 - x - 12}$  in the form  $p + \frac{qx + r}{x^2 - x - 12}$ , where  $p$ ,  $q$  and  $r$  are integers. 1
- (b) Hence express  $\frac{3x^2 + x - 17}{x^2 - x - 12}$  with partial fractions. 3

**Answers****2001**

$$\frac{x}{x^2-1} = \frac{1}{2(x+1)} + \frac{1}{2(x-1)}$$

**2002**

$$y = 1 - \frac{2}{x+1} + \frac{1}{(x+1)^2}$$

**2004**

$$\frac{1}{x^2-x-6} = \frac{1}{5(x-3)} - \frac{1}{5(x+2)}$$

**2005**

$$\frac{1}{x^3+x} = \frac{1}{x} - \frac{x}{x^2+1}$$

**2007**

$$\frac{1}{x} + \frac{2}{x+2} - \frac{1}{x-3}$$

**2008**

$$\frac{4}{x} + \frac{8x}{x^2+5}$$

**2009**

$$\frac{2}{(x+2)^2} + \frac{1}{x-4}$$

**2011**

$$\frac{2}{x-1} - \frac{3}{x+5}$$

**2012**

$$\frac{1}{9} \left( \frac{1}{x-1} - \frac{1}{x+2} - \frac{3}{(x+2)^2} \right)$$

**2014**

$$\frac{3}{(2-3r)} - \frac{1}{(1-r)}$$

**2015**

$$17. \quad 2x + 5 \ln|x-3| + \frac{1}{2} \ln(x^2+1) + k$$

**2016**

$$13. \quad \frac{2}{x+4} + \frac{5}{6-x}$$

**2017**

$$2. \quad \frac{3}{(x+1)} - \frac{2}{(x-2)} + \frac{4}{(x-2)^2} \quad (4)$$

**2018**

$$\frac{1}{x-5} + \frac{2}{x+3}$$

**2019**

$$a) \quad 3 + \frac{4x+19}{x^2-x-12}$$

$$b) \quad 3 - \frac{1}{x+3} + \frac{5}{x-4}$$