

Advanced Higher Maths
SQA 2018 Paper
Question 11



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- (a) Obtain the matrix, A , associated with an anticlockwise rotation of $\frac{\pi}{3}$ radians about the origin. 1
- (b) Find the matrix, B , associated with a reflection in the x -axis. 1
- (c) Hence obtain the matrix, P , associated with an anticlockwise rotation of $\frac{\pi}{3}$ radians about the origin followed by reflection in the x -axis, expressing your answer using exact values. 2
- (d) Explain why matrix P is not associated with rotation about the origin. 1
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Answers/method:

(a)
$$\begin{pmatrix} \cos \frac{\pi}{3} & -\sin \frac{\pi}{3} \\ \sin \frac{\pi}{3} & \cos \frac{\pi}{3} \end{pmatrix}$$

(b)
$$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

(c)
$$\frac{1}{2} \begin{pmatrix} 1 & -\sqrt{3} \\ -\sqrt{3} & -1 \end{pmatrix}$$

- (d) Compare the elements of P with the general form of a rotation matrix, and conclude that they are inconsistent.