

Advanced Higher Maths  
SQA 2019 Paper  
Question 2

Matrix  $A$  is defined by

$$A = \begin{pmatrix} 2 & 1 & 4 \\ -3 & p & 2 \\ -1 & -2 & 5 \end{pmatrix}$$

where  $p \in \mathbb{R}$ .

(a) Given that the determinant of  $A$  is 3, find the value of  $p$ .

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Matrix  $B$  is defined by

$$B = \begin{pmatrix} 0 & 1 \\ q & 3 \\ 4 & 0 \end{pmatrix}$$

where  $q \in \mathbb{R}$ .

(b) Find  $AB$ .

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(c) Explain why  $AB$  does not have an inverse.

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Answers:

(a)  $-3$

(b)  $\begin{pmatrix} q+16 & 5 \\ -3q+8 & -12 \\ -2q+20 & -7 \end{pmatrix}$

(c)  $A$  has order  $3 \times 3$  and  $B$  has order  $3 \times 2$ , so  $AB$  has order  $3 \times 2$ , which isn't a square matrix. Only square matrices can have inverses.