

Advanced Higher Homework 5

1. Differentiate the following functions with respect to x :

(a) $y = x^2 \sin^{-1} x^3$ (b) $y = x^4 \tan^{-1}(1 - x)$ (c) $y = \tan^{-1}\left(\frac{2x}{3}\right)$

(d) $y = \sin^{-1}\left(\frac{x}{4}\right)$ (e) $y = \tan^{-1}\left(\frac{x-4}{x+4}\right)$ (f) $y = \sin^{-1}\left(\frac{x-9}{x+9}\right)$

2. (a) Use implicit differentiation to find $\frac{dy}{dx}$ if $4x^2 + 9xy + 5y^2 = 3$.

(b) Hence find the equation of the tangent at the point $(-2, 1)$ on the curve $4x^2 + 9xy + 5y^2 = 3$.

3. Find the gradient of the tangent to the curve $\sin x + 4 \cos y = 2\sqrt{3}$ at the point $(0, \frac{\pi}{6})$.