## Maths.scot

## National 5 Maths

## Simultaneous Equations

## SQA past paper and specimen paper questions and answers by topic

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Brian and Bob visit a ski resort. Brian buys 3 full passes and 4 restricted passes. The total cost of his passes is $£ 185$.
(a) Write down an equation to illustrate this information.
(b) Bob buys 2 full passes and 3 restricted passes.

The total cost of his passes is $£ 130$.
Write down an equation to illustrate this information.
(c) Find the cost of a restricted pass and the cost of a full pass.

Answers:
Choosing $f$ for the price of a full pass and $r$ for price of a restricted pass:
(a) $3 f+4 r=185$
(b) $2 f+3 r=130$
(c) Restricted pass: $£ 20$. Full pass: $£ 35$.

Two groups of people go to a theatre.
Bill buys tickets for 5 adults and 3 children.
The total cost of his tickets is $£ 158 \cdot 25$.
(a) Write down an equation to illustrate this information.
(b) Ben buys tickets for 3 adults and 2 children.

The total cost of his tickets is $£ 98$.
Write down an equation to illustrate this information.
(c) Calculate the cost of a ticket for an adult and the cost of a ticket for a child.

Answers:
Choosing $a$ for the price of an adult ticket and $c$ for price of a child's ticket:
(a) $5 a+3 c=158.25$
(b) $3 a+2 c=98$
(c) Adult ticket: $£ 22.50$. Child's ticket: $£ 15.25$.

Solve algebraically the system of equations

$$
\begin{aligned}
& 3 x+2 y=17 \\
& 2 x+5 y=4
\end{aligned}
$$

Answer:

$$
x=7, y=-2
$$

Charlie is making costumes for a school show.
One day he made 2 cloaks and 3 dresses.
The total amount of material he used was $9 \cdot 6$ square metres.
(a) Write down an equation to illustrate this information.
(b) The following day Charlie made 3 cloaks and 4 dresses.

The total amount of material he used was 13.3 square metres.
Write down an equation to illustrate this information.
(c) Calculate the amount of material required to make one cloak and the amount of material required to make one dress.

Answers:
Choosing $c$ for the amount of material in one cloak and $d$ for the amount of material in one dress:
(a) $2 c+3 d=9.6$
(b) $3 c+4 d=13.3$
(c) One cloak: $1.5 \mathrm{~m}^{2}$. One dress: $2.2 \mathrm{~m}^{2}$.

The graph below shows two straight lines with the equations:

- $3 x-y=2$
- $x+3 y=19$


The lines intersect at the point P .
Find, algebraically, the coordinates of $P$.

Answer:
$(2.5,5.5)$

Solve, algebraically, the system of equations

$$
\begin{aligned}
& 4 x+5 y=-3 \\
& 6 x-2 y=5
\end{aligned}
$$

Answer:
$x=\frac{1}{2}, y=-1$

# Question 8 

John bought 7 bags of cement and 3 bags of gravel.
The total weight of these bags was 215 kilograms.
(a) Write down an equation to illustrate this information.

Shona bought 5 bags of cement and 4 bags of gravel.
The total weight of her bags was 200 kilograms.
(b) Write down an equation to illustrate this information.
(c) Calculate the weight of one bag of cement and the weight of one bag of gravel.

Answers:
Choosing $c$ for the weight of a bag of cement and $g$ for the weight of a bag of gravel:
(a) $7 c+3 g=215$
(b) $5 c+4 g=200$
(c) Bag of cement: 20 kg . Bag of gravel: 25 kg .

Solve, algebraically, the system of equations

$$
\begin{aligned}
& 5 c+2 d=4 \\
& 4 c-3 d=17
\end{aligned}
$$

Answer:
$c=2, d=-3$

Moira buys 4 mangoes and 3 apples at a fruit shop.
The total cost is $£ 4.25$.
(a) Write down an equation to illustrate this information.

Sami buys 5 mangoes and 2 apples in the same fruit shop.
The total cost is $£ 4.70$.
(b) Write down an equation to illustrate this information.
(c) Calculate, algebraically, the cost of a mango and the cost of an apple.

## Answers:

Choosing $m$ for the price of a mango and $a$ for the price of an apple:
(a) $4 m+3 a=4.25$ (or 425 if working in pence)
(b) $5 m+2 a=4.70$ (or 470 if working in pence)
(c) Mango 80p, apple 35p

Solve, algebraically, the system of equations

$$
\begin{aligned}
& 2 x+3 y=8 \\
& 5 x+2 y=-2
\end{aligned}
$$

Answer:
$x=-2$
$y=4$

