

Name Solutions

Teacher \_\_\_\_\_

## Mathematics Paper 2

### National 5 **Booster Paper C2**

Duration: 1 hour 50 minutes

Total Marks - 60

Attempt ALL questions.

You may use a calculator

To earn full marks, you must show your working in your answers.

State the units for your answer where appropriate.

Write your answers clearly in the spaces provided in this booklet.

Use blue or black ink.

#### Notes:

- This is a **Booster Paper**. Your May exam will be (a bit) harder than this.
- The Booster Papers get **more challenging** as you work through them.
- The final Booster Paper will be as challenging as your May exam.
- The number of marks indicated beside each question is intended as a guide and may differ slightly from SQA marking instructions.
- These original papers are **produced independently of the SQA** and are **free of charge**.
- All Booster Papers and answers can be found at [www.maths180.com/BoosterPapers](http://www.maths180.com/BoosterPapers)

## National 5 Booster Paper C2

1.  $4 \sin x^\circ + 3 = 1$

$$4 \sin x^\circ = -2$$

$$\sin x^\circ = -\frac{2}{4}$$

$$\frac{S}{T} \mid \frac{A}{C}$$

$30^\circ$

$$x = \sin^{-1}\left(-\frac{1}{2}\right)$$

$$= 210^\circ, 330^\circ$$

2.  $A = \frac{1}{2} ab \sin C$

$$= \frac{1}{2} \times 4.5 \times 3.5 \times \sin 110^\circ$$

$$= 7.400079\dots$$

$$= 7.4 \text{ m}^2 \text{ (1dp)}$$

3 a) 10, 11,  $\textcircled{12}$ , 14, 15,  $\vdots$  17, 17,  $\textcircled{18}$ , 18, 19

$Q_1$                        $Q_2$                        $Q_3$

$$\text{Median} = Q_2 = 16$$

$$\begin{aligned} \text{SIQR} &= \frac{Q_3 - Q_1}{2} \\ &= \frac{18 - 12}{2} \\ &= 3 \end{aligned}$$

b) On average, the number of butterflies visiting the garden in 2008 was greater than 2018. ( $16 > 14$ )

In 2008, the number of butterflies visiting the garden was more consistent than in 2018 ( $3 < 5$ )

$$4. \quad \frac{3x+8}{4} + \frac{3x+2}{2} = 8$$

$$\frac{3x+8}{4} + \frac{6x+4}{4} = 8$$

$$\frac{9x+12}{4} = 8$$

$$9x+12 = 32$$

$$9x = 20$$

$$x = \frac{20}{9}$$

$$5. \quad \vec{AF} = \underline{p} + \underline{q}$$

$$\begin{aligned} \vec{EB} &= -\underline{q} - \underline{q} - \underline{p} \\ &= -2\underline{q} - \underline{p} \end{aligned}$$

$$6. \quad 124\% = 49.60$$

$$1\% = 0.4$$

$$100\% = \underline{140}$$

$$7. \quad x^3(2x^5 + x^{-2})$$

$$= 2x^8 + x$$

$$8. \quad \frac{x}{360} \times \pi \times 14 = 16.5$$

$$x = \frac{16.5 \times 360}{14\pi}$$

$$= 135.054 \dots$$

$$= 135^\circ \text{ (to nearest degree)}$$

$$9. \quad y = 9x^2 - 12x + 4$$

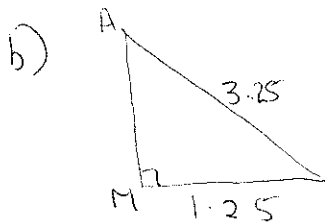
$$\begin{aligned} a &= 9 & b^2 - 4ac \\ b &= -12 & = (-12)^2 - 4(9)(4) \\ c &= 4 & = 144 - 144 \\ & & = 0 \end{aligned}$$

Since  $b^2 - 4ac = 0$  then there is only one real root

$$\begin{aligned} 10. \quad vsf &= \frac{625}{135} & lsf &= \sqrt[3]{\frac{125}{27}} \\ &= \frac{125}{27} & &= \frac{5}{3} \end{aligned}$$

$$\begin{aligned} \text{Height} &= \frac{5}{3} \times 12 \\ &= 20 \text{ cm} \end{aligned}$$

$$\begin{aligned} 11. \quad a) \quad OM &= 3.25 - 2 \\ &= 1.25 \text{ m} \end{aligned}$$



$$\begin{aligned} AM^2 &= 3.25^2 - 1.25^2 \\ &= 9 \end{aligned}$$

$$\begin{aligned} AM &= \sqrt{9} \\ &= 3 \text{ m} \end{aligned}$$

$$\begin{aligned} \therefore AB &= 2 \times 3 \text{ m} \\ &= 6 \text{ m} \end{aligned}$$

$$12. \quad \cos \hat{CAB} = \frac{15^2 + 11^2 - 7^2}{2 \times 15 \times 11}$$

$$= 0.9$$

$$\hat{CAB} = \cos^{-1}(0.9)$$

$$= 25.8419 \dots$$

$$= 25.8^\circ \text{ (1dp)}$$

$$13. \quad 3x^2 - 4x - 8 = 0$$

$$a = 3 \quad b = -4 \quad c = -8$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{4 \pm \sqrt{16 - 4(3)(-8)}}{6}$$

$$= \frac{4 \pm \sqrt{112}}{6}$$

$$\Rightarrow \frac{4 + \sqrt{112}}{6}$$

$$= 2.4305 \dots$$

$$= 2.43$$

$$\text{or } \frac{4 - \sqrt{112}}{6}$$

$$= -1.09716 \dots$$

$$= -1.10$$

$$14. \quad \frac{1}{4x} + \frac{8}{x} = 11$$

$$\Rightarrow \frac{1}{4x} + \frac{32}{4x} = 11$$

$$\frac{33}{4x} = 11$$

$$44x = 33$$

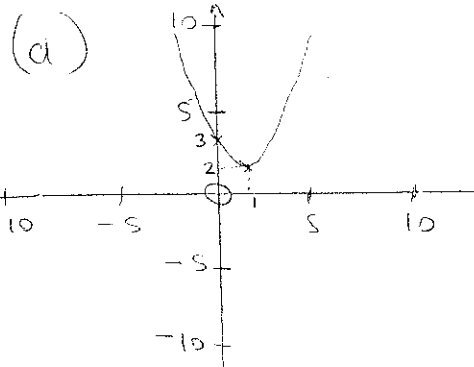
$$x = \frac{3}{4}$$

$$15. \quad a = 4, \quad b = 2, \quad c = 1$$

16 (a)  $(1, 2)$

(b)  $x = 1$

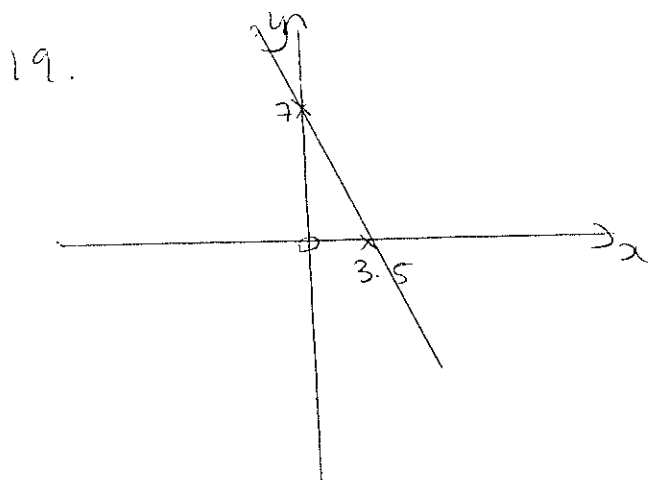
(c)  $(0, 3)$



17.  $AC = \frac{20}{15} \times 9$   
 $= 12 \text{ cm}$

$BC = 12 - 9$   
 $= 3 \text{ cm}$

18.  $\frac{\cos x^2 \left( \frac{\sin x^2}{\cos x^2} \right)}{\sin x^2}$   
 $= \frac{\sin x^2}{\sin x^2}$   
 $= 1$



(crosses  $x$ -axis when  $y = 0$ )

$$0 = -2x + 7$$

$$2x = 7$$

$$x = 3.5 \quad (3.5, 0)$$

(crosses  $y$ -axis when  $x = 0$ )

$$y = -2(0) + 7$$

$$y = 7 \quad (0, 7)$$