

National 5

Exam Solutions

SQA Exam 2018 Solutions

Paper 1

1. $\frac{7}{3} + \frac{4}{5}$

$$\frac{7 \times 5}{3 \times 5} + \frac{4 \times 3}{5 \times 3}$$

$$\frac{35}{15} + \frac{12}{15} = \frac{47}{15} = 3 \frac{2}{15}$$

2 $(3x + 1)(x - 1) + 2(x^2 - 5)$

$$\begin{array}{r} 3x^2 - 3x \\ + x - 1 \\ 2x^2 - 10 \end{array}$$

$$5x^2 - 2x - 11$$

3
$$\begin{array}{r} 4x + 5y = -3 \\ 6x - 2y = 5 \end{array} \quad \begin{array}{l} \textcircled{1} \times 2 \\ \textcircled{2} \times 5 \end{array}$$

$$\begin{array}{r} 8x + 10y = -6 \\ 30x - 10y = 25 \end{array} \quad \begin{array}{l} \textcircled{3} \\ \textcircled{4} \end{array}$$

$$\textcircled{3} + \textcircled{4}$$

$$\begin{array}{r} 38x = 19 \\ x = 0.5 \end{array}$$

Sub $x = 0.5$ into $\textcircled{1}$

$$4x + 5y = -3$$

$$2 + 5y = -3$$

$$5y = -5$$

$$y = -1$$

$$4 \quad \begin{pmatrix} 1 \\ 5 \\ 1 \end{pmatrix} + \begin{pmatrix} - \\ - \\ - \end{pmatrix} = \begin{pmatrix} 6 \\ -4 \\ 3 \end{pmatrix}$$

$$\mathbf{v} = \begin{pmatrix} 5 \\ -9 \\ 2 \end{pmatrix}$$

$$5 \quad \begin{aligned} x^2 - 11x + 24 &= 0 \\ (x-3)(x-8) &= 0 \end{aligned}$$

$$x-3=0 \quad \text{or} \quad x-8=0$$

$$x=3 \quad \text{or} \quad x=8$$

$$6 \quad \text{Graph max}=5, \text{ min} = -5 \quad \Rightarrow a = 5$$

2 waves between 0 and 180 means 4 waves between 0 and 360
 $\Rightarrow b = 4$

$$7 \quad \mathbf{a} \quad m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{20-14}{12-8}$$

$$m = \frac{6}{4} = \frac{3}{2}$$

$$y = mx + c \quad \text{sub in } (8, 14)$$

$$14 = \frac{3}{2} \times 8 + c$$

$$14 = 12 + c$$

$$c = 2$$

$$y = \frac{3}{2}x + 2$$

$$P = \frac{3}{2}d + 2$$

7 **b** $\frac{3}{2} \times 5 + 2$

$7.5 + 2 = \text{£}9.50$

8 $a = 2, \quad b = 4, \quad c = 5$

$b^2 - 4ac$

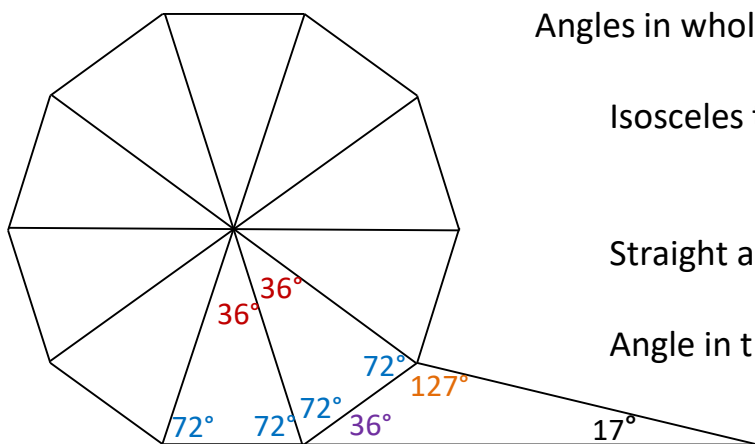
$4^2 - 4 \times 2 \times 5$

$16 - 40 = 24$

$b^2 - 4ac < 0$

No real roots

9



Angles in whole turn $360 \div 10 = 36$

Isosceles triangles $180 - 36 = 144$

$144 \div 2 = 72$

Straight angle $180 - 72 - 72 = 36$

Angle in triangle $180 - 127 - 36 = 17^\circ$

10 use cos rule $a^2 = b^2 + c^2 - 2bc \cos A$

$a^2 = 10^2 + 8^2 - 2 \times 8 \times 10 \times 1/8$

$a^2 = 164 - 2 \times 8 \times 10 \times 1/8$

$a^2 = 164 - 20 = 144$

$a = \sqrt{144}$

$a = 12$

11 $\frac{9 \times \sqrt{6}}{\sqrt{6} \times \sqrt{6}}$

$$\frac{9\sqrt{6}}{6} = \frac{3\sqrt{6}}{2}$$

12 $\cos 60^\circ = 0.5$

Cos is positive in Q1 and Q4

240 is in Q3 (between 180 and 270)

Therefore $\cos 240^\circ = -0.5$

13 Use D (6, 0, 0) (A is 4 along x, so D must be 6)

B(4, 8, 5)

C(6, 8, 0)

14 $y - h = g\sqrt{x}$ (swap sides)

$$\sqrt{x} = \frac{y-h}{g}$$

$$x = \left(\frac{y-h}{g}\right)^2$$

15

$$\left(\frac{2}{3}\right)^2 = \frac{4}{9}$$

$$(p^4)^2 = p^8$$

$$\frac{4}{9}p^8$$

When $x = 0$ (y intercept)

$$y = -6 \times 4 = -24 \quad (0, 24)$$

When $y = 0$ (roots)

$$0 = (x - 6)(x + 4)$$

$$x = 6, x = -4$$

$$(-4, 0)$$

$$(6, 0)$$

Turning point: x value will be in between roots

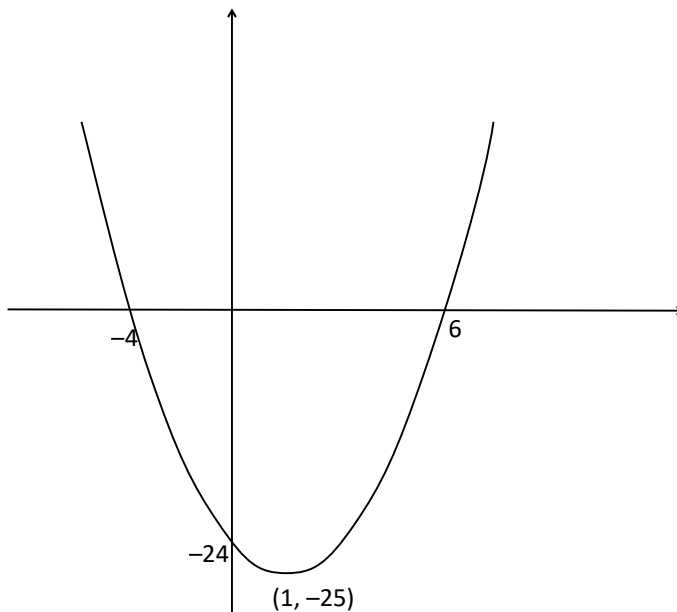
-4 -3 -2 -1 0 1 2 3 4 5 6

$$x = 1$$

$$y = (1 - 6)(1 + 4)$$

$$= -5 \times 5 = -25$$

$$(1, -25)$$



17

$$V = \frac{1}{3} Ah$$

$$\frac{1}{3} 6 \times 6 \times h = 138$$

$$12h = 138$$

$$h = \frac{138}{12} = \frac{69}{6} = \frac{23}{2}$$

$$h = 11.5\text{cm}$$

18

$$\tan x = \frac{\sin x}{\cos x}$$

$$\sin x \cos x \frac{\sin x}{\cos x}$$

$$\sin^2 x$$

19 ai

$$\begin{aligned} (x-3)^2 + q \\ x^2 - 6x + 9 + q \quad 9 + q = -81 \end{aligned}$$

$$(x-3)^2 - 90$$

$$p = 3$$

$$q = -90$$

ii

$$x = 3 \quad (\text{this would make the bracket } (3-3) = 0)$$

b Method 1

$$(x - 3)^2 - 90 = 0$$

$$(x - 3)^2 = 90$$

$$x - 3 = \pm\sqrt{90}$$

$$x = 3 \pm \sqrt{90}$$

$$x = 3 \pm \sqrt{9}\sqrt{10}$$

$$x = 3 \pm 3\sqrt{10}$$

Method 2 (probably used more)

$$a = 1, \quad b = -6 \quad c = -81$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{6 \pm \sqrt{(-6)^2 - 4 \times 1 \times -81}}{2}$$

$$\frac{6 \pm \sqrt{36 + 324}}{2}$$

$$\frac{6 \pm \sqrt{360}}{2}$$

$$\frac{6 \pm \sqrt{36}\sqrt{10}}{2}$$

$$\frac{6 \pm 6\sqrt{10}}{2}$$

$$3 \pm 3\sqrt{10}$$

Paper 2

1. Fall by 2% = $100 - 2 = 98\%$

2018, 2019, 2020 = 3 years

$$125\,000 \times 0.98^3$$

117 649 tonnes

2 $r = 7.4$

$d = 14.8$

$$\frac{320}{360} \times \pi \times 14.8$$

41.32939 cm

(41.308444 cm)

3

$$|r| = \sqrt{24^2 + (-12)^2 + 8^2}$$

$$|r| = \sqrt{789}$$

$$|r| = 28$$

4 $3x < 6x - 6 - 12$

$$3x < 6x - 18$$

$$18 < 3x$$

$$6 < x$$

$$x > 6$$

5

$$\bar{x} = \frac{756}{6} = 126$$

x	\bar{x}	$x - \bar{x}$	$(x - \bar{x})^2$
120	126	-6	36
126	126	0	0
125	126	-1	1
124	126	-2	4
130	126	4	16
131	126	5	25
			82

$$s = \sqrt{\frac{\sum(x - \bar{x})^2}{n-1}}$$

$$s = \sqrt{\frac{82}{5}}$$

$$s = \sqrt{16.4}$$

$$s = 4.04969$$

b

Mean has reduced => On average less people visited on Sunday

S.D has increased => Amount of visitors to different stalls less consistent on Sunday
(or visitors to stalls on Sunday more spread)

6

$$f(a) = 5 + 4a = 73$$

$$4a = 68$$

$$a = 17$$

$$7 \quad V = \frac{4}{3} \pi r^3$$

$$V = 4 \div 3 \times \pi \times 3 \cdot 2^3$$

$$V = 137.258 \quad (137.18869)$$

$$V = 140\text{cm}^3$$

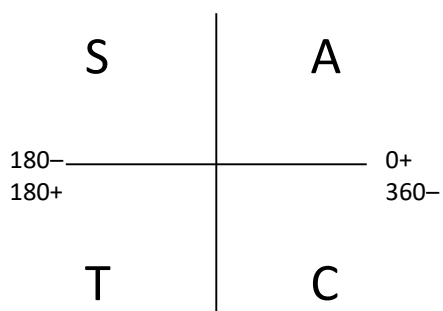
8

$$7 \sin x + 2 = 3$$

$$7 \sin x = 1$$

$$\sin x = \frac{1}{7}$$

$$\begin{aligned} \text{Base angle } x &= \sin^{-1}(1/7) \\ x &= 8.2^\circ \end{aligned}$$



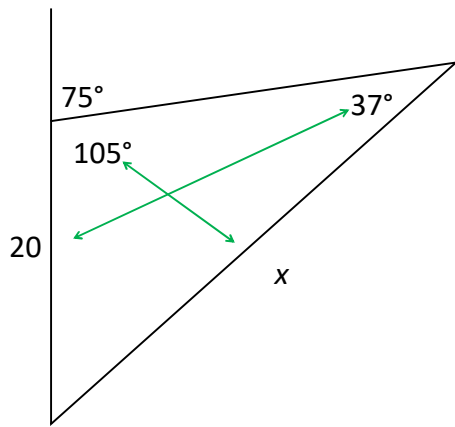
$\sin x$ is positive (1/7 is positive)

$\sin x$ is positive in Q1 and Q2

$$\text{In Q1} \quad x = 8.2^\circ$$

$$\text{In Q2} \quad x = 180 - 8.2 = 171.8^\circ$$

9



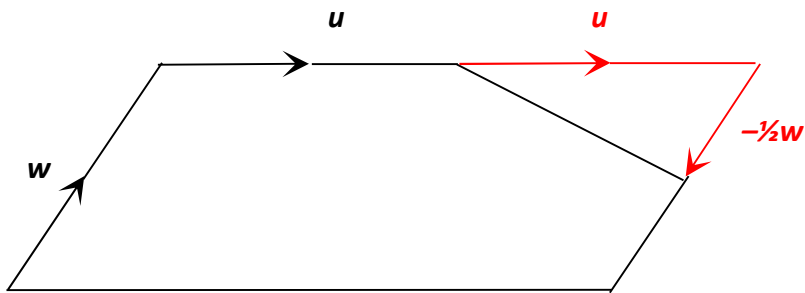
$$180 - 75 = 105$$

$$\frac{x}{\sin 105} = \frac{20}{\sin 37}$$

$$x = \frac{20 \sin 105}{\sin 37}$$

$$x = 32.1 \text{ cm}$$

10



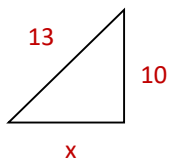
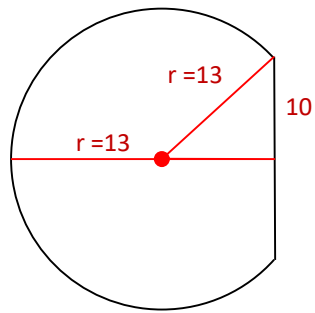
$$BC = u - \frac{1}{2}w$$

11 85% = 9.3×10^{11}

$$100\% = (9.3 \times 10^{11}) \div 0.85$$

$$= 1.094117647 \times 10^{12} \text{ km}^3$$

12



$$x^2 = 13^2 - 10^2$$

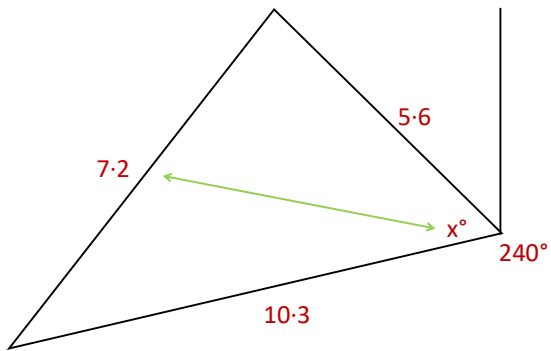
$$x^2 = 69$$

$$x = \sqrt{69}$$

$$x = 8.3066 \text{ cm} \quad (\text{use } 8.3)$$

$$\text{Width} = 13 + 8.3$$

$$= 21.3 \text{ cm}$$



$$\cos X = \frac{b^2 + c^2 - a^2}{2bc}$$

$$\cos X = \frac{10.3^2 + 5.6^2 - 7.2^2}{2 \times 10.3 \times 5.6}$$

$$\cos X = \frac{85.61}{115.36}$$

$$\cos X = 0.75$$

$$X = 42.088$$

$$= 42.1^\circ$$

$$\text{Bearing} = 240 + 42.1$$

$$= 282.1^\circ$$

14 On y axis $x = 0$

$$2x - 5y = 20$$

$$-5y = 20$$

$$y = -4 \qquad (0, -4)$$

15

$$\frac{n}{n^2 - 4} \div \frac{3}{n - 2}$$

$$\frac{n}{n^2 - 4} \times \frac{n - 2}{3}$$

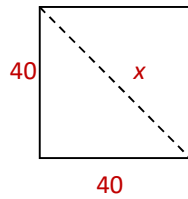
$$\frac{n(n - 2)}{3(n^2 - 4)}$$

$$\frac{n(n - 2)}{3(n - 2)(n + 2)}$$

$$\frac{n}{3(n + 2)}$$

16. Method 1 Repeated Pythagoras

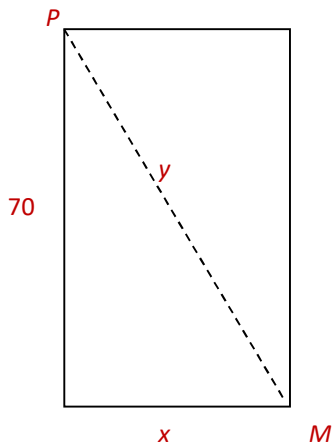
Base of cuboid



$$x^2 = 40^2 + 40^2$$

$$x^2 = 3200$$

Cross Section of Cuboid



$$y^2 = x^2 + 70^2$$

$$y^2 = 3200 + 4900$$

$$y^2 = 8100$$

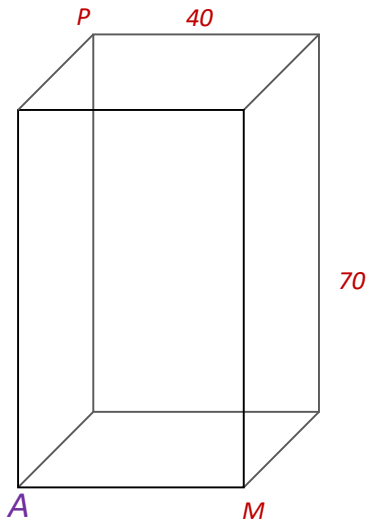
$$y = 90 \text{ cm}$$

PM is the largest space for a straight object to go.

PM = 90cm which is larger than 85 cm so

The umbrella will fit

16. Method 2 3D Coordinates/ Vector Magnitude



Assume point A (0, 0, 0)

Therefore M(40, 0, 0)

P(0, 40, 70)

$$\vec{MP} = \begin{pmatrix} 70 - 0 \\ 40 - 0 \\ 0 - 40 \end{pmatrix} = \begin{pmatrix} 70 \\ 40 \\ -40 \end{pmatrix}$$

$$|\vec{MP}| = \sqrt{70^2 + 40^2 + (-40)^2}$$

$$|\vec{MP}| = \sqrt{8100}$$

$$|\vec{MP}| = 90$$

PM is the largest space for a straight object to go.

PM = 90cm which is larger than 85 cm so

The umbrella will fit

17.

$$\begin{aligned}\text{Area of triangle} &= \frac{1}{2} ab \sin C \\ &= \frac{1}{2} 38 \times 55 \times \sin 75 \\ &= 1009.392488\end{aligned}$$

$$\begin{aligned}\text{Area of sector} &= \frac{75}{360} \times \pi r^2 \\ &= \frac{75}{360} \times \pi \times 30^2 \\ &= 589.0486225 \quad (588.75)\end{aligned}$$

$$\begin{aligned}\text{Shaded Area} &= \text{Sector} - \text{Triangle} \\ &= 420.3438655 \text{ cm}^2 \quad (420.642488)\end{aligned}$$

18 a

$$\text{Scale Factor (Length)} = \frac{24}{16} = 1.5$$

$$\text{Corresponding Volume Scale Factor} = 1.5^3 = 3.375$$

If these shapes were mathematically similar then

$$V_{\text{Large}} \text{ should be equal to } V_{\text{Small}} \times 3.375.$$

$$V_{\text{Large}} = 1125\text{cm}^3$$

$$\begin{aligned} V_{\text{Small}} \times 3.375 &= 576 \times 3.375 \\ &= 1944 \text{ cm}^3 \end{aligned}$$

Since these are not equal,
The cartons are not mathematically similar

$$\mathbf{b} \quad \text{Volume Scale Factor} = \frac{1500}{576}$$

$$\text{Scale Factor} = \sqrt[3]{\frac{1500}{576}} = 1.3758$$

$$\begin{aligned} \text{New Depth} &= \text{Depth}_{\text{small}} \times \text{Scale Factor} \\ &= 16 \times 1.3758 \quad (16 \times \text{Ans on calc}) \\ &= 22.012848326 \text{ cm} \end{aligned}$$